Version 1.0



General Certificate of Education (A-level) June 2012

Mathematics

MPC1

(Specification 6360)

Pure Core 1





PMT

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Key to mark scheme abbreviations

М	mark is for method
m or dM	mark is dependent on one or more M marks and is for method
А	mark is dependent on M or m marks and is for accuracy
В	mark is independent of M or m marks and is for method and accuracy
E	mark is for explanation
\sqrt{or} ft or F	follow through from previous incorrect result
CAO	correct answer only
CSO	correct solution only
AWFW	anything which falls within
AWRT	anything which rounds to
ACF	any correct form
AG	answer given
SC	special case
OE	or equivalent
A2,1	2 or 1 (or 0) accuracy marks
-x EE	deduct <i>x</i> marks for each error
NMS	no method shown
PI	possibly implied
SCA	substantially correct approach
с	candidate
sf	significant figure(s)
dp	decimal place(s)

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

MPC1				1
Q	Solution	Marks	Total	Comments
1	$\frac{5\sqrt{3}-6}{2\sqrt{3}+3} \times \frac{2\sqrt{3}-3}{2\sqrt{3}-3}$	M1		
1	$2\sqrt{3}+3$ $2\sqrt{3}-3$	1411		
	(Numerator =) $30 - 15\sqrt{3} - 12\sqrt{3} + 18$	m1		$\operatorname{correct}(=48-27\sqrt{3})$
	(Denominator = 12 - 9 =) 3	B1		must be seen as denominator
	$\left(\frac{48-27\sqrt{3}}{3}\right) = 16-9\sqrt{3}$	A1	4	CSO; accept $16 + -9\sqrt{3}$
	$\begin{pmatrix} 3 \end{pmatrix}^{-10}$	AI	4	$CSO, accept 10 + - 9\sqrt{3}$
	Total		4	
				$y = \pm \frac{4}{3}x + k$
2(a)(i)	$y = \frac{4}{3}x - \frac{7}{3}$	M1		5
_()(-)	3 3			or $\frac{\Delta y}{\Delta x}$ with 2 correct points
	4			
	\Rightarrow grad $AB = \frac{4}{3}$	A1	2	condone slip in rearranging if gradient is correct; condone 1.33 or better
	3			
(ii)	y = 'their grad' $x + c$			
	and attempt to use $x = 3$, $y = -5$	M1		or $y5 =$ 'their grad $AB'(x - 3)$
				or $4x - 3y = k$ and attempt to find k using
				x = 3 and $y = -5$
	$y+5 = \frac{4}{3}(x-3)$ or $y = \frac{4}{3}x - \frac{27}{3}$			compact equation in any form but must
	$\begin{array}{c} 3 \\ 4 \\ 27 \end{array}$	A1		correct equation in any form but must simplify $-$ to $+$
	or $y = \frac{1}{3}x - \frac{27}{3}$			
	5 5	A 1	2	integer coefficients in required form
	4x - 3y = 27	A1	3	eg $-8x + 6y = -54$
	4x - 3y = 7 and $3x - 2y = 4$			must use compating in of a susting and
(b)	$\Rightarrow 8x - 9x = 14 - 12 \text{ etc}$	M1		must use correct pair of equations and attempt to eliminate <i>x</i> or <i>y</i> (generous)
	x = -2	A1		accompt to emininate x or y (generous)
	y = -5	A1	3	or $D(-2,-5)$
			5	(-, -)
(c)	4(k-2)-3(2k-3)=7			sub $x = k - 2$, $y = 2k - 3$ into $4x - 3y = 7$
(-)	4(k-2)-3(2k-3)=7 4k-8-6k+9=7			and attempt to multiply out with all k
		M1		terms on one side (condone one slip)
	$\Rightarrow k = -3$	A1	2	
	Total		10	

MPC1				
Q	Solution	Marks	Total	Comments
3(a)(i)	$p(-1) = (-1)^3 + 2(-1)^2 - 5(-1) - 6$	M1		p(-1) attempted not long division
	$p(-1) = -1 + 2 + 5 - 6 = 0 \implies x + 1$ is a factor	A1	2	CSO; correctly shown = 0 plus statement
(ii)	Quad factor in this form: $(x^2 + bx + c)$	M1		long division as far as constant term <i>or</i> comparing coefficients, <i>or</i> $b = 1$ <i>or</i> $c = -6$ by inspection
	$x^2 + x - 6$	A1		correct quadratic factor
	$\left[p(x)=\right](x+1)(x+3)(x-2)$	A1	3	must see correct product
(b)	p(0) = -6; $p(1) = -8$	M1		both $p(0)$ and $p(1)$ attempted and at least one value correct
	$\Rightarrow p(0) > p(1)$	A1	2	AG both values correct plus correct statement involving p(0) and p(1)
(c)	y t /	M1 A1		cubic with one max and one min \bigwedge with $-3, -1, 2$ marked
	-3 -1 2 x	A1	3	correct with minimum to right of <i>y</i> -axis AND going beyond –3 and 2
	Total		10	

0	Solution	Marks	Total	Comments
4(a)(i)	$3x^2 + 3x^2 + xy + xy + 3xy + 3xy$	M1		correct expression for surface area
	$6x^2 + 8xy = 32$			$2(3x^2 + xy + 3xy) = 32$ etc
	$\Rightarrow 3x^2 + 4xy = 16$	A1	2	AG be convinced
(ii)	$(V =)3x^2y$ OE	M1		correct volume in terms of x and y
	$= 3x \left(\frac{16 - 3x^2}{4}\right) \text{ or } = 3x^2 \left(\frac{16 - 3x^2}{4x}\right)$			OE
	$=12x-\frac{9x^3}{4}$	A1	2	CSO AG be convinced that all working is correct
(b)	$\left(\frac{\mathrm{d}V}{\mathrm{d}x}\right) = 12 - \frac{27}{4}x^2$	M1 A1	2	one of these terms correct all correct with 9×3 evaluated (no + c etc)
(c)(i)	$x = \frac{4}{3} \Longrightarrow \frac{\mathrm{d}V}{\mathrm{d}x} = 12 - \frac{27}{4} \times \left(\frac{4}{3}\right)^2$	M1		attempt to sub $x = \frac{4}{3}$ into ' <i>their</i> ' $\frac{dV}{dx}$
	$\frac{\mathrm{d}V}{\mathrm{d}x} = 12 - \frac{27}{4} \times \frac{16}{9} = 12 - 12$			or $12 - \frac{432}{36} = 12 - 12$ or $12 - \frac{48}{4} = 0$ etc
	$\frac{\mathrm{d}V}{\mathrm{d}x} = 0 \implies \text{stationary value}$	A1	2	CSO; shown = 0 plus statement
(ii)	$\frac{\mathrm{d}^2 V}{\mathrm{d}x^2} = -\frac{27x}{2} \qquad \mathrm{OE}$	B 1√		FT for ' <i>their</i> ' $\frac{dV}{dx} = a + bx^2$
	when $x = \frac{4}{3}$, $\frac{d^2 V}{dx^2} < 0 \implies \text{maximum}$	E1√	2	or sub of $x = \frac{4}{3}$ into <i>'their'</i> $\frac{d^2 V}{dx^2}$ \Rightarrow maximum
	$\left(\text{FT "minimum" if their } \frac{d^2 V}{dx^2} > 0 \right)$			E0 if numerical error seen
	Total		10	

MPC1				
Q	Solution	Marks	Total	Comments
5(a)(i)	$\left(x-\frac{3}{2}\right)^2$	M1		or $p = 1.5$ stated
	$\left(x-\frac{3}{2}\right)^2+\frac{11}{4}$	A1	2	$(x-1.5)^2 + 2.75$
	Mark their final line as their answer			
(ii)	$x = \frac{3}{2}$	B1√	1	correct or FT their " $x = p$ "
(b)(i)	$x^2 - 3x + 5 = x + 5 \Longrightarrow x^2 = 4x$	M1		eliminating <i>x</i> or <i>y</i> and collecting like terms (condone one slip)
				or $(y-5)^2 - 3(y-5) + 5 = y$
				$\Rightarrow y^2 - 14y + 45 = 0$
	$(x \neq 0) \qquad \Rightarrow x = 4$	A1		
	$ (x \neq 0) \qquad \Longrightarrow x = 4 y = 9 $	A1	3	
(**)	$\frac{x^3}{3} - \frac{3x^2}{2} + 5x(+c)$	M1		one of these terms correct
(11)	$\frac{-}{3} - \frac{-}{2} + 5x(+c)$	A1 A1	3	another term correct all correct (need not have $+ c$)
		211	5	
(iii)	$\left[\right]_{0}^{4} = \frac{4^{3}}{3} - 3 \times \frac{4^{2}}{2} + 5 \times 4$	M1		must have earned M1 in part(b)(ii) $F(\text{their } x_B) \{-F(0)\}$ "correctly sub'd"
	$=17\frac{1}{3}$	A1		$\left(\frac{64}{3} - 24 + 20\right) = \frac{52}{3}$ or $\frac{104}{6}$ etc
				condone 17.3 but not $16\frac{4}{3}$ etc
	Area trapezium $=\frac{1}{2}(x_B)(5+y_B)$	B1√		FT their numerical values of x_B , y_B
				Area = $\frac{1}{2} \times 4 \times 14$ (= 28)
	Area of shaded region = $28 - 17\frac{1}{3}$			
	$=10\frac{2}{3}$	A1	4	CSO; $\frac{32}{3}$, accept 10.7 or better
	Total		13	

MPC1				
Q	Solution	Marks	Total	Comments
6(a)	$\left(x-5\right)^2+\left(y-8\right)^2$	B1		
	= 25	B1	2	condone 5 ²
(b)(i)	$(2-5)^2 + (12-8)^2$			or $AC^2 = 3^2 + 4^2$
	=9+16 = 25 $\Rightarrow A \text{ lies on circle}$	B1	1	hence $AC = 5$; (also radius = 5) CSO
	(must have concluding statement and circle equation correct if using equation)			$(\Rightarrow \text{ radius } = AC) \Rightarrow A \text{ lies on circle}$ (must have concluding statement & RHS of circle equation correct or $r = 5$ stated if Pythagoras is used)
(ii)	grad $AC = -\frac{4}{3}$	B1		
	Gradient of tangent is $\frac{3}{4}$	B 1√		FT their $-1/$ grad AC
	y-12 = 'their tangent grad' (x-2)	M1		or $y =$ 'their tangent grad' $x + c$ & attempt to find <i>c</i> using $x = 2$, $y = 12$
	$y-12 = \frac{3}{4}(x-2)$ or $y = \frac{3}{4}x + \frac{21}{2}$ etc	A1		correct equation in any form
	3x - 4y + 42 = 0	A1	5	CSO; must have integer coefficients with all terms on one side of equation accept $0 = 8y - 6x - 84$ etc
(c)(i)	$(CM^2 =)$ $(7-5)^2 + (12-8)^2$	M1		or $(CM^2 =)$ 20
	$ \begin{pmatrix} CM^2 = \end{pmatrix} (7-5)^2 + (12-8)^2 \left(\Rightarrow CM = \sqrt{20} \right) \Rightarrow (CM =) 2\sqrt{5} $	A1	2	
(ii)	$PM^2 = PC^2 - CM^2 = 25 - 20$	M1		Pythagoras used correctly
				eg $d^2 + (2\sqrt{5})^2 = 5^2$
	$\Rightarrow PM = \sqrt{5}$	A1		
	Area $\Delta PCQ = \sqrt{5} \times 2\sqrt{5}$ = 10	Δ 1	2	CSO
	= 10 Total	A1	3 13	

$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	Comments t interpretation of y increasing ee at least one of these steps before nswer for A1 G no errors in working t factors or correct use of quadratic $10 \pm \sqrt{4}$
(ii) $(3x-4)(x-2)$ (10x - 3x ² - 8) > 0 $\Rightarrow 3x^2 - 10x + 8 < 0$ A1 2 CSO A minute set final an CSO A	nswer for A1 G no errors in working t factors or correct use of quadratic
(ii) $(3x-4)(x-2)$ M1 correct	t factors or correct use of quadratic
(ii) $(3x-4)(x-2)$ M1 equation	
	on formula as far as $\frac{10 \pm \sqrt{4}}{6}$
CVs are $\frac{4}{3}$ and 2 A1 condor	here $\frac{8}{6}$ and $\frac{12}{6}$ here but not in final
3 AI line	6 6
$ \xrightarrow{1}{4} \xrightarrow{2}{2} \xrightarrow{+} \xrightarrow{+} \xrightarrow{-} \xrightarrow{+} \xrightarrow{+} \xrightarrow{+} \xrightarrow{-} \xrightarrow{+} \xrightarrow{+} \xrightarrow{+} \xrightarrow{+} \xrightarrow{+} \xrightarrow{+} \xrightarrow{+} +$	or sign diagram
$\frac{4}{3} < x < 2$ A1 4 or 2>	$x > \frac{4}{3}$
	$x < 2$ AND $x > \frac{4}{3}$
but not Mark their final line as their answer	t $x < 2$ OR $x > \frac{4}{3}$
nor x	$x < 2$, $x > \frac{4}{3}$

MPC1				
Q	Solution	Marks	Total	Comments
7(b)(i)	$x = 2 ; \left(\frac{\mathrm{d}y}{\mathrm{d}x}\right) = 40 - 24 - 16$	M1		sub $x = 2$ into $\frac{dy}{dx}$ and simplify terms
	$\frac{dy}{dx} = 0 \implies$ tangent at <i>P</i> is parallel to	A1	2	must be all correct working plus statement
	the <i>x</i> -axis			du
(ii)	$x = 3; \frac{dy}{dx} = 20 \times 3 - 6 \times 3^{2} - 16$ (= 60-54-16) = -10	M1		must attempt to sub $x = 3$ into $\frac{dy}{dx}$
		A1		
	Gradient of normal $=\frac{1}{10}$	A1√		$\frac{-1}{"their -10"}$
	Normal: $(y - 1) = $ 'their grad' $(x - 3)$	m1		normal attempted with correct coordinates
				used and gradient obtained from their $\frac{dy}{dx}$
				value
	$y+1 = \frac{1}{10}(x-3)$	A1		any correct form, eg $10y = x - 13$ but must simplify $$ to $+$
	(Equation of tangent at P is) $y = 3$	B1		
	<i>x</i> = 43	A1	7	$CSO; \Rightarrow R(43,3)$
	Total		15	
	TOTAL		75	